# Modeling vectorborne diseases

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## Vector-borne diseases

#### Mosquitos

- 🗆 Malaria
- Heartworm
- West Nile Virus
- Yellow fever
- Ticks
  - Lyme disease
  - Ehrlichiosis
  - □ Tick-borne relapsing fever



#### Standard model based on malaria

#### Epidemiology of malaria

- Several disease agents
  - Protozoan parasites
    - □ Plasmodium vivax, P. falciparum, P. ovale, P. malariae
- Transmitted by female mosquitoes via blood meal
- Mosquitoes infectious after disease agent completes growth cycle
  - 9-21 days at 25 C (shorter at higher temps)
- 7-30 day incubation period in host after bite before symptoms appear
- Parasites can remain dormant in host and re-activate periodically

# Assumptions of basic model

- No host immunity
- No disease-associated mortality in host or vector
- No latent state for host or vector
- Constant population size
  Birth rate = death rate
- Newborns are susceptible



- Vector life-span <<< host life-span</p>
- Concept: 2 separate populations (host & vector) that affect each other

#### Basic vector-borne disease model



# Definitions

- a = # bites on host per time period
- b = vector infectivity
  - P(host infection | vector infectious)
- m = biting vector:host ratio
- ŷ = proportion of infectious vectors (vector disease prevalence)
- y = proportion of infectious hosts (host disease prevalence)

## Definitions, continued

#### c = host infectivity

- □ P(vector infection | host infectious)
- proportion of susceptible vector bites on infectious host that produce vector infection

#### • $\gamma$ = rate of recovery from infection

- $\Box$  = 1/D (duration of infection)
- $\mu$  = rate of death in vector population
  - $\Box$  = 1/L (vector life expectancy)
- N = Density of host population

 $\square N = X + Y$ 

•  $\hat{N}$  = Density of vector population  $\hat{N} = \hat{X} + \hat{Y}$ 

## What affects host incidence?

#### Host incidence increases with

- □ Bites/host in time period
- □ Vector infectivity
- Vector:host ratio
- Disease prevalence in vector
- Host incidence decreases with
  - Disease prevalence in host (decreased probability that bitten host is uninfected)
- Host prevalence decreases with
  - Duration of infection

## What affects vector incidence?

Vector incidence increases with Bites/host in time period □ Host infectivity Disease prevalence in host Vector incidence decreases with Disease prevalence in vector (decreased) probability that biting vector is uninfected)

# Which parameters might be targets for control measures?

- Bites/host (a)
  - Bug sprays, i.e. DEET products
- Vector infectivity (b)
  - □ Host vaccine programs
- Vector:host ratio (m)
  - Environmental insect control programs

#### Rate of change in host prevalence:

$$\frac{dy}{dt} = abm\hat{y}(1-y) - \gamma y \qquad \text{Incidence rate} \\ - \text{recovery rate} \end{cases}$$

#### Rate of change in vector prevalence:

$$\frac{d\hat{y}}{dt} = acy(1-\hat{y}) - \mu\hat{y}$$
 Incidence rate  
- death rate

# R<sub>0</sub> for vector-borne diseases

- Number of secondary cases per primary case in a susceptible population
- Product of host-tovector transmission (R<sub>V0</sub>) and vector-to-host transmission (R<sub>H0</sub>)



# R<sub>0</sub> for vector-borne diseases

- Number of vector cases per host (R<sub>V0</sub>) □ amc/γ
  - Bites/vector \* vectors/host \* host infectivity \* duration of host infectivity
- Number of host cases per vector (R<sub>H0</sub>) ab/µ

Bites/vector \* vector infectivity \* lifespan of vector

# R<sub>0</sub> for vector-borne diseases

#### Overall rate is R<sub>V0</sub> \* R<sub>H0</sub>:

$$\frac{amc}{\gamma} * \frac{ab}{\mu} = \frac{ma^2bc}{\mu\gamma} = R_0$$

Note the importance of "a":
 Number of bites on host

# Stability (endemic state)

- Occurs when rate of change in host and vector populations is 0
- Useful for determining
  - □ Whether an endemic state can develop
  - □ Vector / host prevalence in endemic state

# Stability

• Host stability: 
$$abm\hat{y}(1-y) - \gamma y = 0$$
  
 $abm\hat{y} = \frac{\gamma y}{1-y}$ 

Vector stability: 
$$acy(1-\hat{y}) - \mu \hat{y} = 0$$
  
 $acy = \frac{\mu \hat{y}}{1-\hat{y}}$ 

 Solve for y and ŷ to determine equilibrium prevalence

## Prevalence at equilibrium

• Host:  $y^* = \frac{(R_0 - 1)}{\left[R_0 + \frac{ac}{\mu}\right]}$ 

• Vector: 
$$\hat{y}^* = \left(\frac{(R_0 - 1)}{R_0}\right) \left(\frac{\frac{ac}{\mu}}{1 + \frac{ac}{\mu}}\right)$$

# Macdonald's stability index

#### ■ ac/µ

- Larger value suggests endemic disease
- Smaller value suggests epidemic outbreaks that die off
- Larger value when:
  - □ Many bites/host
  - □ High P(vector infection | host infected)
  - Long vector lifespan
- Reported values from 0.47 to 4.9 for malaria in Africa

#### Spreadsheet model – user inputs

User inputs					
Time step (in 10-day units	)		dt	0.1	
Vector biting rate per day			а	4	
Proportion of bites that infect host			b	0.1	
Proportion of bites that infect vector			с	0.1	
Life expectancy of vectors			L	2	
Duration of host infectiousness (% vector life expectancy)		D	3		
Number of hosts			Ν	1000	
Number of vectors			Nhat	100000	
Infected host population t=0			Y <sub>0</sub>	100	
Infected vector population t=0			Yhat₀	1000	

# Spreadsheet model – calculated parameters

Parameters calculated from user inputs					
Vector-to-host density	m	100			
Vector mortality rate	mu	0.5			
Host infectious recovery ra	ite gamma	0.33333			
Host basic reproductive ra	te R <sub>H0</sub>	0.8			
Vector basic reproductive	rate R <sub>v₀</sub>	120.0			
Basic reproductive rate	$R_{o}$	96.0			
MacDonald's stability index	c	0.8			

#### Spreadsheet model - exploration

# Spreadsheet model - results

Equilibrium values			
Parameter	CA	LCULATED	OBSERVED
Number infected hosts at equilibriu	n	981.4	981.4
Number infected vectors at equilibri	um	43981.5	43981.5
% hosts infected at equilibrium		0.981	0.981
% vectors infected at equilibrium		0.440	0.440

### Spreadsheet model - results



## Expansion beyond the basic model

- Latent periods in vector and host
- Seasonal changes in mosquito population
- Co-infections in humans
- Acquired immunity

## References

 Anderson RM, May RM, <u>Infectious Diseases of Humans:</u> <u>Dynamics and Control</u>. 1991. Oxford University Press. Pp 392-419.